
CH B – THE COORDINATE PLANE

Someone once said, “A picture is worth a thousand words.” This is especially true in math, where many ideas are very abstract. The French mathematician-philosopher René Descartes (“*I think, therefore I am*”) devised a way for us to visually represent the solutions of many kinds of equations. It’s called the ***Cartesian Coordinate System***. [The term *Cartesian* is the Latin form of the name Descartes.]

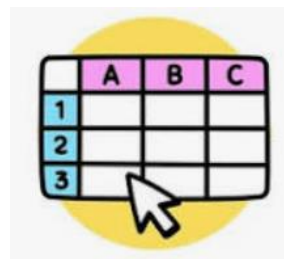


We’ve seen one-dimensional number lines before.

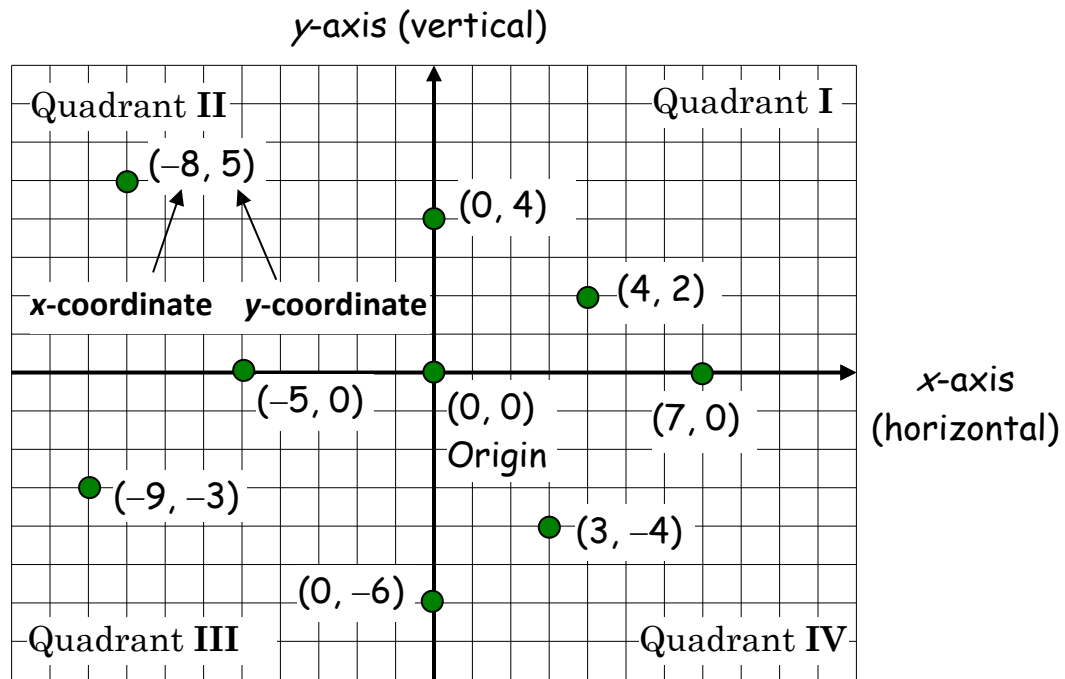


In this chapter, we take two number lines (one called the x-axis and one called the y-axis), line them up perpendicular to each other (90° angle between them), and we have a two-

dimensional system sometimes called ***2-space***. It’s a fancy form of the “Battleship” game, or the basic layout of a spreadsheet.



❑ THE CARTESIAN COORDINATE SYSTEM (2-SPACE)



Observations on 2-Space

1. A two-dimensional coordinate system represents a **plane**. The horizontal axis is called the **x -axis** in math, but will be called other things in other subjects. Similarly, the vertical **y -axis** will be called something else in other subjects.
2. The **ordered pair (x, y)** represents a single **point** in the plane. The numbers x and y in the ordered pair are the **coordinates** of that point. Notice that a single point (ordered pair) consists of two coordinates. [The coordinates of a point on the Earth are called its longitude and latitude.]
3. The point **$(0, 0)$** , where the axes intersect (cross), is called the **origin**.



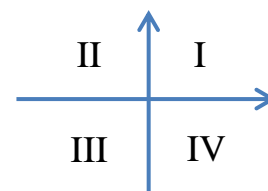
4. The first coordinate of the point (x, y) represents the distance to the right or left from the origin. The second coordinate represents the distance up or down. For example, the point $(3, -4)$ is plotted by starting at the origin, moving 3 units to the right, and then moving 4 units down.
5. The **quadrants** are numbered I (one) through IV (four), starting in the upper-right region and going counterclockwise.

In Quadrant I, both coordinates (the x and y) are positive.

In Quadrant II, x is negative and y is positive.

In Quadrant III, both coordinates are negative.

In Quadrant IV, x is positive and y is negative.



6. Points on the x -axis or the y -axis are not in any quadrant.
7. Every point on the x -axis has a y -coordinate of 0.
Every point on the y -axis has an x -coordinate of 0.

Homework

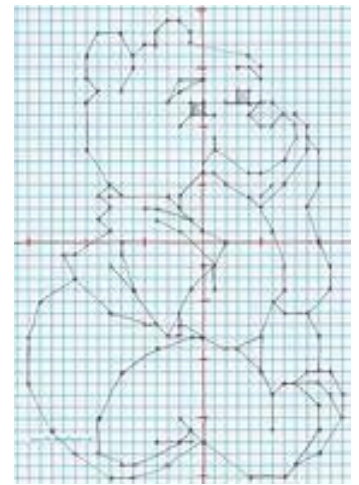
1. Is the Cartesian coordinate system described in this chapter 1-, 2-, or 3-dimensional?
2.
 - a. Does the notation (x, y) represent one point or two points?
 - b. Does the notation (x, y) represent one coordinate or two coordinates?
3.
 - a. The point $(7, -\sqrt{3})$ lies in Quadrant ____.
 - b. The point $(-\pi, -9)$ lies in Quadrant ____.
 - c. The point $(-1, \sqrt{2})$ lies in Quadrant ____.
 - d. The point $(\pi, \sqrt{5})$ lies in Quadrant ____.

4.
 - a. The point $(17, 0)$ lies on the ____ axis.
 - b. The point $(0, -20)$ lies on the ____ axis.
 - c. The point $(0, 0)$ is called the ____ and lies on the ____ axis.

5.
 - a. In Quadrant I, x is ____ and y is ____.
 - b. In Quadrant II, x is ____ and y is ____.
 - c. In Quadrant III, x is ____ and y is ____.
 - d. In Quadrant IV, x is ____ and y is ____.

6.
 - a. In which quadrants are the signs of x and y the same?
 - b. In which quadrants are the signs of x and y opposites?

7.
 - a. A point lies on the x -axis. What can you say for sure about the coordinates of that point? Hint: The following are points on the x -axis: $(7, 0)$, $(-23, 0)$, and $(\pi, 0)$.
 - b. A point lies on the y -axis. What can you say for sure about the coordinates of that point?
 - c. A point lies on both axes. What can you say for sure about the coordinates of that point?



❑ GEOGRAPHY

One last connection between the x - y coordinate system and the longitude/latitude system used on the Earth: The x -axis can be thought of as the *Equator* (0° latitude), and the y -axis can be viewed as the *Prime Meridian* (0° longitude), a line of longitude going from the North Pole to the South Pole and passing through Greenwich, England, just outside London.

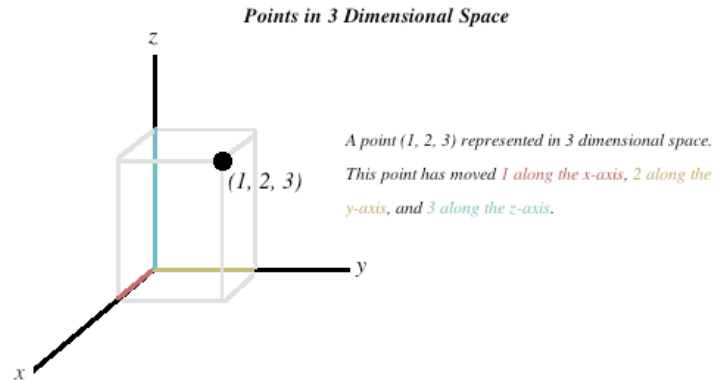


Review Problems

8.
 - a. The y -axis is the (horizontal, vertical) axis.
 - b. In the point $(7, 9)$, the x -coordinate is _____.
 - c. The point $(0, 0)$ is called the _____.
 - d. In which quadrant is x positive and y negative?
 - e. Every point on the y -axis has an x -coordinate of _____.
 - f. Which quadrant is the point $(-\pi, \sqrt{17})$ in?

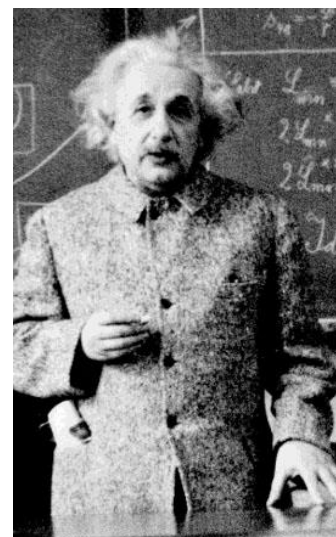
Solutions

1. The Cartesian coordinate system in this course is **2**-dimensional. A **1**-dimensional coordinate system might be the x -axis. In later courses, you might encounter a **3**-dimensional coordinate system, and if you major in math or physics, you will find even higher-dimension coordinate systems, including an infinite-dimensional coordinate system!



2. a. one b. two
3. a. IV b. III c. II d. I
4. a. x b. y c. origin; it's on both axes.
5. a. positive; positive b. negative; positive
c. negative; negative d. positive, negative
6. a. I and III b. II and IV
7. a. The y -coordinate must be 0.
b. The x -coordinate must be 0.
c. Both coordinates must be 0, since it's the origin.
8. a. vertical b. 7 c. origin
d. IV e. 0 f. II

“Where the world ceases to be the scene of our personal hopes and wishes, where we face it as free beings admiring, asking and observing, there we enter the realm of Art and Science.”



Albert Einstein
(1879-1955)